



## Antiferromagnetism in $\text{EuPdGe}_3$



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### ABSTRACT

The results of X-ray diffraction, magnetic susceptibility and magnetization, and <sup>151</sup>Eu Mössbauer spectroscopy measurements of polycrystalline  $\text{EuPdGe}_3$  are reported.  $\text{EuPdGe}_3$  crystallizes in the  $\text{BaNiSn}_3$ -type tetragonal structure (space group  $I4mm$ ) with the lattice constants  $a = 4.4457(1)$  Å and  $c = 10.1703(2)$  Å. The results are consistent with  $\text{EuPdGe}_3$  being an antiferromagnet with the Néel temperature  $T_N = 12.16(1)$  K and with the Eu spins  $S = 7/2$  in the  $ab$  plane. The temperature dependence of the magnetic susceptibility above  $T_N$  follows the modified Curie-Weiss law with the effective magnetic moment of  $7.82(1)$   $\mu_B$  per Eu atom and the paramagnetic Curie temperature of  $-5.3(1)$  K indicative of dominant antiferromagnetic interactions. The  $M(H)$  isotherms for temperatures approaching  $T_N$  from above are indicative of dynamical short-range antiferromagnetic ordering in the sample. The temperature dependence of the hyperfine magnetic field follows a  $S = 7/2$  Brillouin function. The principal component of the electric field gradient tensor is shown to increase with decreasing temperature and is well described by a  $T^{3/2}$  power-law relation. The Debye temperature of  $\text{EuPdGe}_3$  determined from the Mössbauer data is  $199(2)$  K.

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## 1. Introduction

There are more than 100 ternary compounds of the general chemical formula  $\text{XYZ}_3$  that crystallize in different crystal structure types [1,2]. The largest number of  $\text{XYZ}_3$  compounds crystallizes in the  $\text{BaNiSn}_3$ -type crystal structure [3], which belongs to the tetragonal space group  $I4mm$  (No. 107). Among the  $\text{BaNiSn}_3$ -type compounds, the most intensively studied are those exhibiting superconductivity, heavy-fermion or Kondo lattice characteristics:  $\text{LaIrSi}_3$  [4–8],  $\text{LaRhSi}_3$  [5–7,10–13],  $\text{LaPdSi}_3$  [14,15],  $\text{LaPtSi}_3$  [15],  $\text{CeIrSi}_3$  [7,8,16–21,9,22–33],  $\text{CeRhSi}_3$  [7,16,11,17,18,21,34–49],  $\text{CeCoSi}_3$  [6,21,50–57],  $\text{CeIrGe}_3$  [16,21,9,57–62],  $\text{CeRhGe}_3$  [16,21,60,58,63],  $\text{CeCoGe}_3$  [58,57,64–72],  $\text{CeFeGe}_3$  [73–75],  $\text{BaPtSi}_3$  [76,77],  $\text{CaYSi}_3$  ( $Y = \text{Ir, Pt}$ ) [78],  $\text{SrYGe}_3$  ( $Y = \text{Pd, Pt}$ ) [77] and  $\text{SrAuSi}_3$  [79]. Other compounds of the  $\text{BaNiSn}_3$  structure type, such as  $\text{CeCuZ}_3$  ( $Z = \text{Al, Ga}$ ) [80],  $\text{XIrSi}_3$  ( $X = \text{Gd, Tb, Dy}$ ) [81,82],  $\text{GdCoSi}_3$  [54,83],  $\text{GdYGe}_3$  ( $Y = \text{Ni, Cu}$ ) [83],  $\text{GdCuAl}_3$  [83],  $\text{XCoGe}_3$  ( $X = \text{Pr, Nd}$ ) [84],  $\text{EuPtZ}_3$  ( $Z = \text{Si, Ge}$ ) [85,86],  $\text{XPdGe}_3$  ( $X = \text{La, Eu}$ ) [87,88],  $\text{EuNiGe}_3$  [90,89] and  $\text{LaOsSi}_3$  [91], are also reported and studied for their interesting physical properties. The presence of a very

wide range of elements in the selected  $\text{BaNiSn}_3$ -type compounds indicated above point to the possibility of discovering new isostructural compounds of this type.

In this paper, we report on the synthesis and the results of crystallographic, magnetic, and <sup>151</sup>Eu Mössbauer spectroscopy investigations of a polycrystalline  $\text{EuPdGe}_3$  compound. We demonstrate that this compound exhibits a long-range antiferromagnetic order below  $T_N = 12.16(1)$  K with the Eu magnetic moments lying in the  $ab$  plane. We provide evidence for the presence of short-range antiferromagnetic correlations above  $T_N$ . We show that magnetic and Mössbauer data are consistent with the Eu atoms having spin 7/2. We find that the Debye temperature of  $\text{EuPdGe}_3$  is  $199(2)$  K.

## 2. Experimental methods

The polycrystalline sample of  $\text{EuPdGe}_3$  was prepared using the constituent elements of Eu (purity 99.9%), Pd (purity 99.99%), and Ge (purity 99.999%) in stoichiometric ratio. Appropriate amounts of these elements were welded under a purified argon atmosphere into a tantalum container. The container in turn was held within an evacuated fused silica jacket to avoid its air oxidation. The mixture was melted at  $1050$  °C for 4 h, followed by annealing at  $600$  °C for 190 h, and then quenching into cold water.

X-ray diffraction measurements were performed at  $298$  K in Bragg–Brentano geometry on the PANalytical X'Pert scanning diffractometer using  $\text{Cu K}\alpha$  radiation in the  $2\theta$  range  $15$ – $111.5^\circ$  in steps of  $0.02^\circ$ . The  $K\beta$  line was eliminated by using a Kevex PSI2 Peltier-cooled solid-state Si detector.

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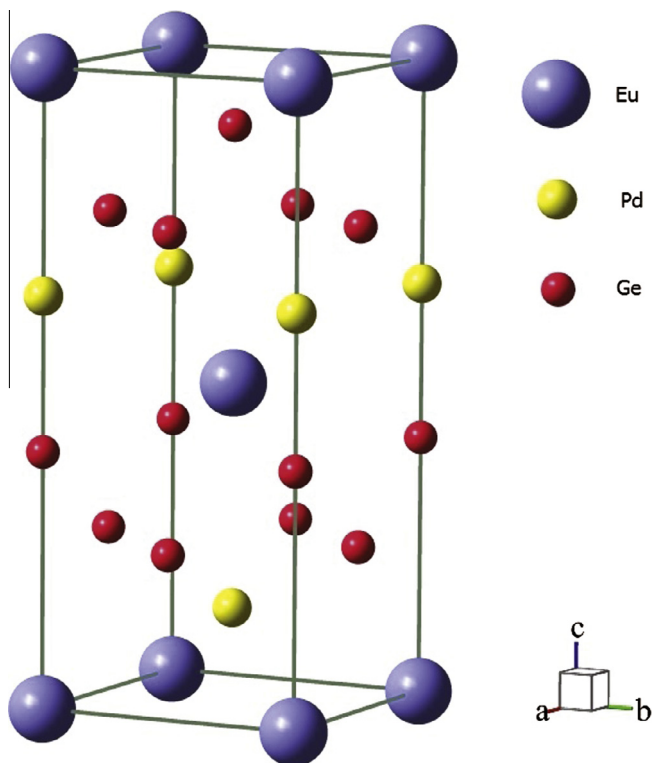


Fig. 1. The unit cell of the  $\text{EuPdGe}_3$  compound.

**Table 1**  
Atomic positions for the tetragonal  $\text{EuPdGe}_3$  obtained through Rietveld analysis.

Atom	Site	Point symmetry (mm)	Occupancy	x	y	z
Eu	2a	4	1.0	0	0	0
Pd	2a	4	1.0	0	0	0.645(2)
Ge	4b	2	1.0	0	$\frac{1}{2}$	0.257(2)
Ge	2a	4	1.0	0	0	0.403(2)

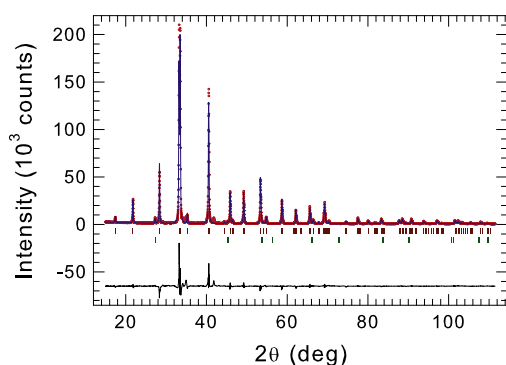


Fig. 2. The X-ray diffraction spectrum of the compound  $\text{EuPdGe}_3$  at 298 K. The experimental data are denoted by open circles, while the line through the circles represents the results of the Rietveld refinement. The upper set of vertical bars represents the Bragg peak positions corresponding to the  $\text{EuPdGe}_3$  phase, while the lower set refers to the positions of the impurity phase of Ge (space group  $Fd\bar{3}m$ ). The lower solid line represents the difference curve between experimental and calculated spectra.

The dc magnetization was measured in the temperature range 2–300 K and in magnetic fields up to 90 kOe using the vibrating sample magnetometer (VSM) option of the Quantum Design physical property measurement system (PPMS). The dc magnetic susceptibility was measured using PPMS in magnetic fields of 100 and 1000 Oe in the temperature range of 2–300 K. The ac magnetic

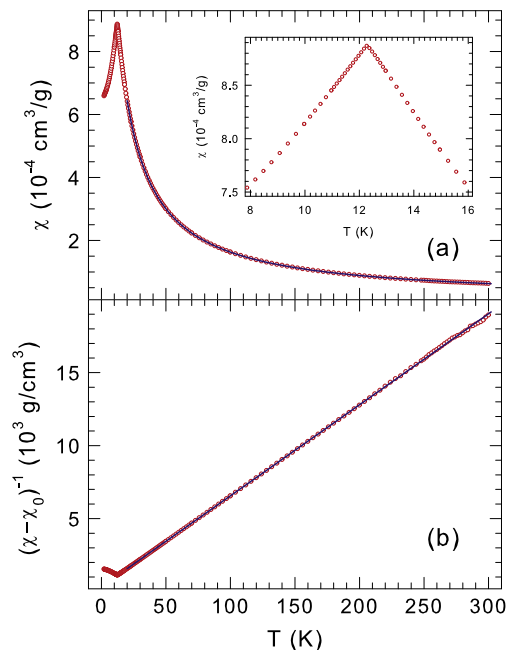


Fig. 3. (a) The temperature dependence of the magnetic susceptibility of  $\text{EuPdGe}_3$ , measured in an external magnetic field of 1000 Oe. The solid line is the fit to Eq. (1) in the temperature range 50–300 K, as explained in the text. The inset shows the magnetic susceptibility data in the low-temperature range. (b) The inverse magnetic susceptibility corrected for the contribution  $\chi_0$ ,  $(\chi - \chi_0)^{-1}$  versus temperature  $T$ . The solid line is the fit to Eq. (1).

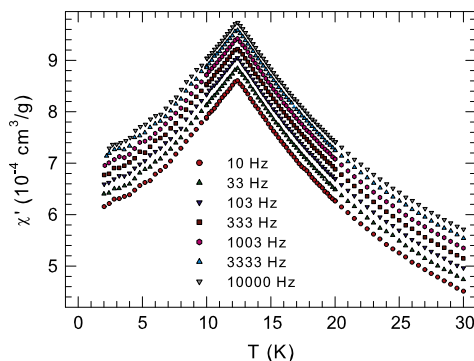


Fig. 4. Temperature dependence of the in-phase component  $\chi'$  of the ac magnetic susceptibility of  $\text{EuPdGe}_3$  for different applied frequencies from 10 to 10,000 Hz. As all these  $\chi'(T)$  curves overlap, they are shifted upward with respect to each other by  $2 \times 10^{-5} \text{ cm}^3/\text{g}$ .

susceptibility data were collected using PPMS between 2.0 and 30 K in a 10 Oe ac magnetic field and zero external dc magnetic field for frequencies varying from 10 Hz to 10 kHz.

The  $^{151}\text{Eu}$  Mössbauer measurements were conducted using a standard, constant acceleration Mössbauer spectrometer operating in sine mode and a  $^{151}\text{Sm}(\text{SmF}_3)$  source at room temperature. The 21.5 keV  $\gamma$ -rays were detected with a proportional counter. The spectrometer was calibrated with a Michelson interferometer [92], and the spectra were folded. The Mössbauer absorber consisted of a mixture of powder  $\text{EuPdGe}_3$  and boron nitride, which was pressed into a pellet that was put into an Al disk container of thickness 0.008 mm to ensure a uniform temperature over the whole sample. The surface density of the Mössbauer absorber was  $28.5 \text{ mg}/\text{cm}^2$ . This corresponds to an effective thickness parameter [93]  $T = 4.1f_a$ , where  $f_a$  is the Debye–Waller factor of the absorber. Since  $T > 1$ , the resonance line shape of the Mössbauer spectra was described using a transmission integral formula [94].

The Mössbauer source  $^{151}\text{Sm}(\text{SmF}_3)$  used is not a monochromatic source as  $^{151}\text{Sm}$  nuclei are located in the  $\text{SmF}_3$  matrix at a site of noncubic symmetry. By measuring the  $^{151}\text{Eu}$  Mössbauer spectra of a cubic  $\text{EuSe}$  compound we determined that the electric quadrupole coupling constant [93]  $eQ_p V_{zz}$  (here  $e$  is the proton charge,  $Q_p = 0.903 \text{ b}$  (Ref. [95]) is the ground-state electric quadrupole moment of the  $^{151}\text{Eu}$  nucleus, and  $V_{zz}$  is the principal component of the electric field gradient (EFG)

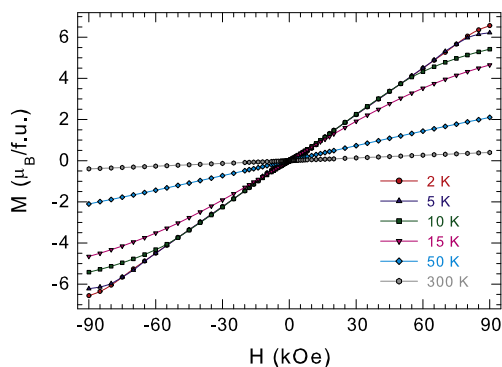


Fig. 5. Magnetization  $M$  versus applied magnetic field  $H$  isotherms of  $\text{EuPdGe}_3$  measured at the indicated temperatures.

tensor) in our source is  $-3.69(13)$  mm/s, which is close to the value of  $-3.6$  mm/s found in Ref. [96]. The precise shape of the source emission line was taken into account in the fits of the  $^{151}\text{Eu}$  Mössbauer spectra. The isomer shift  $\delta$  of the  $^{151}\text{Eu}$  Mössbauer spectra is given here relative to the  $^{151}\text{Sm}(\text{SmF}_3)$  source at room temperature.

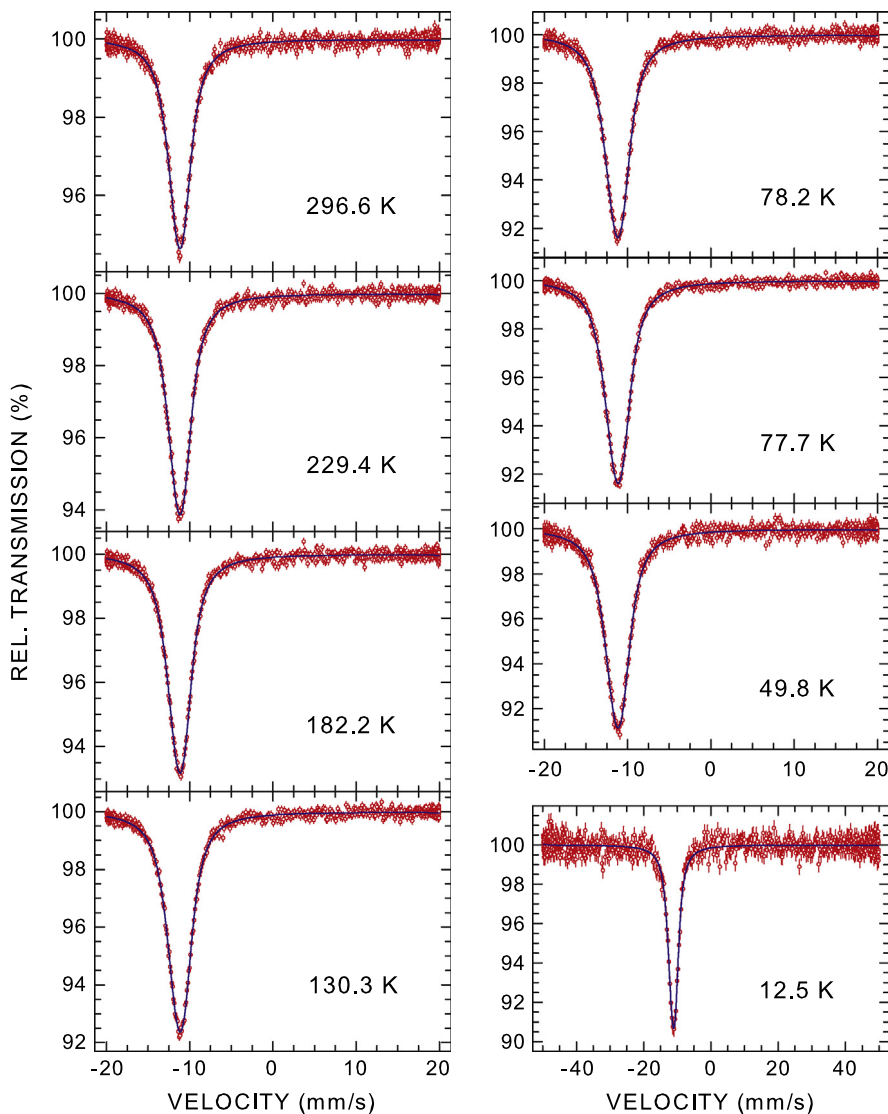


Fig. 6.  $^{151}\text{Eu}$  Mössbauer spectra of  $\text{EuPdGe}_3$  obtained at the indicated temperatures, fitted (solid lines) with an electric quadrupole hyperfine interaction, as described in the text. The zero-velocity origin is relative to the source.

### 3. Experimental results and discussion

#### 3.1. Structural characterization

The ternary compound  $\text{EuPdGe}_3$  crystallizes in the  $\text{BaNiSn}_3$ -type crystal structure with the tetragonal space group  $I4mm$  (No. 107) [97]. There are two formula units of  $\text{EuPdGe}_3$  per unit cell. The crystal structure of  $\text{EuPdGe}_3$  is shown in Fig. 1, with the crystallographic data for the Eu, Pd, and Ge sites listed in Table 1.

The room-temperature X-ray diffraction pattern of  $\text{EuPdGe}_3$  is shown in Fig. 2. A Rietveld refinement [98] of the spectrum in Fig. 2 yields the lattice constants  $a = 4.4457(1)$  Å and  $c = 10.1703(2)$  Å. The values of these lattice parameters compare well with the corresponding values reported earlier [88,97]. As determined from the Rietveld refinement (Fig. 2), the  $\text{EuPdGe}_3$  specimen contains a second phase of Ge (space group  $Fd\bar{3}m$ ) in the amount of 1.0(2) wt%.

#### 3.2. Magnetic measurements

The temperature dependence of the magnetic susceptibility  $\chi$  of  $\text{EuPdGe}_3$  measured in an applied magnetic field of 1000 Oe is

shown in Fig. 3(a) (the identical  $\chi(T)$  data were also obtained in an applied magnetic field of 100 Oe). The sharp peak at  $T_N = 12.27(10)$  K in the  $\chi(T)$  data is indicative of antiferromagnetic ordering occurring at this temperature.

The  $\chi(T)$  data above 50 K (Fig. 3(a)) could be fitted to a modified Curie–Weiss law

$$\chi = \chi_0 + \frac{C}{T - \Theta_p}, \quad (1)$$

where  $\chi_0$  is the temperature-independent term that includes contributions from Pauli and Van Vleck paramagnetism as well as core and Landau diamagnetism,  $C$  is the Curie constant, and  $\Theta_p$  is the paramagnetic Curie temperature. The Curie constant can be expressed as  $C = \frac{N\mu_{\text{eff}}^2}{3k_B}$ , where  $N$  is the number of Eu ions per formula unit,  $\mu_{\text{eff}}$  is the effective magnetic moment, and  $k_B$  is the Boltzmann constant. Fig. 3(b) shows the inverse magnetic susceptibility corrected for the contribution  $\chi_0$  as  $(\chi - \chi_0)^{-1}$  versus temperature; the validity of the modified Curie–Weiss law is evident. The values of  $\chi_0$ ,  $C$ , and  $\Theta_p$  obtained from the fit are, respectively,  $1.06(1) \times 10^{-5}$  cm<sup>3</sup>/g,  $16.04(3) \times 10^{-3}$  cm<sup>3</sup> K/g, and  $-5.3(1)$  K. The value of  $C$  corresponds to  $\mu_{\text{eff}} = 7.82(1) \mu_B$  per Eu atom.

For a free Eu<sup>2+</sup> ion (electronic configuration  $^8S_{7/2}$ ), the theoretical value of  $\mu_{\text{eff}}^{\text{th}} = g\mu_B\sqrt{J(J+1)}$  is  $7.94 \mu_B$  [99]. The fact that the experimental value  $\mu_{\text{eff}} = 7.82(1) \mu_B$  is close to the theoretical value of  $7.94 \mu_B$  confirms that the magnetic moment is localized on the divalent Eu ions. The negative value of  $\Theta_p$  indicates the predominantly antiferromagnetic interaction between the Eu<sup>2+</sup> magnetic moments.

Although the presence of a sharp peak in the  $\chi(T)$  data is a necessary condition for the occurrence of antiferromagnetism, it is not a sufficient condition since a sharp peak in  $\chi(T)$  is also observed for spin-glass compounds [100,101]. We therefore measured the temperature dependence of the in-phase component  $\chi'$  of the ac magnetic susceptibility of EuPdGe<sub>3</sub> for selected frequencies between 10 and 10,000 Hz (Fig. 4). It is clear that the temperature of the maximum in  $\chi'(T)$  curves does not depend on the frequency of the applied ac magnetic field, in contrast to its frequency dependence observed for spin glasses [100,101]. This confirms that the studied compound is an antiferromagnet.

The magnetization  $M$  versus applied magnetic field  $H$  isotherms of EuPdGe<sub>3</sub> at six temperatures between 2 and 300 K are shown in Fig. 5. It is seen from Fig. 5 that at 300 and 50 K the  $M$  exhibits a linear  $H$  dependence. However, the  $M(H)$  curve for  $T = 15$  K, i.e. slightly above  $T_N$ , has a downward curvature. This downward curvature is most probably due to dynamical short-range antiferromagnetic ordering in the sample on approaching  $T_N$  from above [90]. The presence of such a downward curvature in the  $M(H)$  isotherms below  $T_N$  at  $T = 2, 5$  and  $10$  K (Fig. 5) can be explained as being caused by a series of field-induced first-order spin-flop transitions where the ordered magnetic moments flop to a perpendicular orientation with respect the applied field [90]. It is a series of field-induced first-order spin-flop transitions occurring at increasing magnetic fields, rather than one first-order spin-flop transition in a single crystal occurring at a single magnetic field along the easy axis, because of the random orientation of the crystallites in the polycrystalline sample [90].

The maximum observed magnetization of  $6.56 \mu_B/\text{Eu}$  at  $T = 2$  K and  $H = 90$  kOe (Fig. 5) is rather close to the saturation magnetization ( $M_{\text{sat}} = gS\mu_B$ ) of  $7 \mu_B/\text{Eu}$  expected for the free Eu<sup>2+</sup> ion with  $S = 5/2$  and  $g = 2$ . Within the mean-field theory, the critical field  $H_c$  at which  $M$  reaches  $M_{\text{sat}}$  with increasing  $H$  is equal to  $M_{\text{sat}}/\chi(T_N)$ . By taking the  $\chi(T_N)$  value from Fig. 3, one obtains  $H_c = 93$  kOe. This is close to the value of  $\sim 100$  kOe estimated from an extrapolation of the  $T = 2$  K isotherm (Fig. 5) to the value  $M_{\text{sat}} = 7\mu_B$ .

### 3.3. Mössbauer spectroscopy

The <sup>151</sup>Eu Mössbauer spectra of EuPdGe<sub>3</sub> recorded at temperatures at which no magnetic dipole hyperfine interaction [93] is present are shown in Fig. 6. These spectra are in a form of a broadened single line. The Eu atoms in EuPdGe<sub>3</sub> are located at the  $2a$  site with the point symmetry  $4/m\bar{m}$  (Table 1), which ensures a non-zero, axially symmetric (the asymmetry parameter  $\eta = 0$ ) EFG tensor at this site, and hence a non-zero electric quadrupole hyperfine interaction [93]. The spectra in Fig. 6 thus result from a pure electric quadrupole hyperfine interaction [102]. They were analyzed by means of a least-squares fitting procedure which entailed calculations of the positions and relative intensities of the absorption lines by numerical diagonalization of the full hyperfine interaction Hamiltonian [93]. The fit of the 296.6 K Mössbauer spectrum yields  $eQ_g V_{zz} = 3.65(23)$  mm/s and  $\delta = -11.23(1)$  mm/s. The value of  $\delta$  proves that Eu is divalent in the studied compound [102].

The principal component of the EFG tensor  $V_{zz}$  derived from the fits of the spectra in Fig. 6 clearly increases with decreasing temperature [Fig. 7(a)]. In the traditional [103], i.e., not based on a first-principles method [104], interpretation of  $V_{zz}$  one uses the formula

$$V_{zz} = (1 - \gamma_\infty)V_{zz}^{\text{ext}} + (1 - R)V_{zz}^{\text{local}}, \quad (2)$$

where  $V_{zz}^{\text{ext}}$  is a contribution due to external (point) charges,  $V_{zz}^{\text{local}}$  is a contribution due to local charges (caused by valence and conduction electrons near the probe site),  $\gamma_\infty$  and  $R$  are, respectively, Steinheimer antishielding and shielding factors that account for the amplification or attenuation of  $V_{zz}$  resulting from the deformation of closed shells induced by  $V_{zz}^{\text{ext}}$  and  $V_{zz}^{\text{local}}$ , respectively. For Eu<sup>2+</sup> ions with the  $^8S_{7/2}$  ground state, the  $V_{zz}^{\text{local}}$  contribution is negligible and thus any  $V_{zz}$  must arise from the  $V_{zz}^{\text{ext}}$  contribution [105].

An increase of  $V_{zz}$  with decreasing temperature found here [Fig. 7(a)], was also observed in many other crystalline, amorphous, and quasicrystalline compounds [103,106–109]. Although

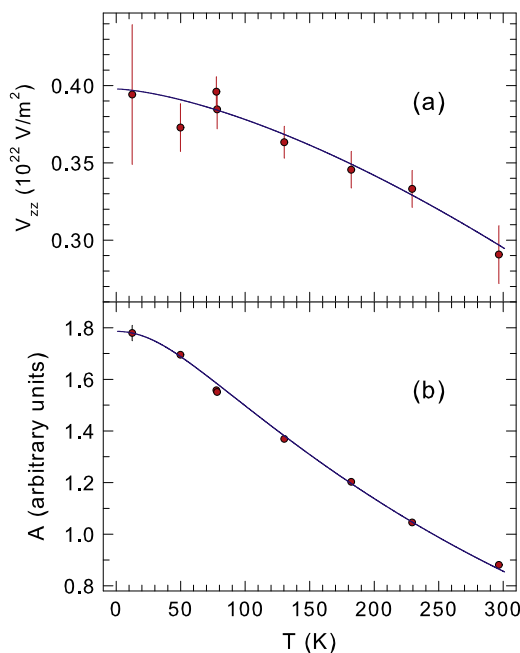
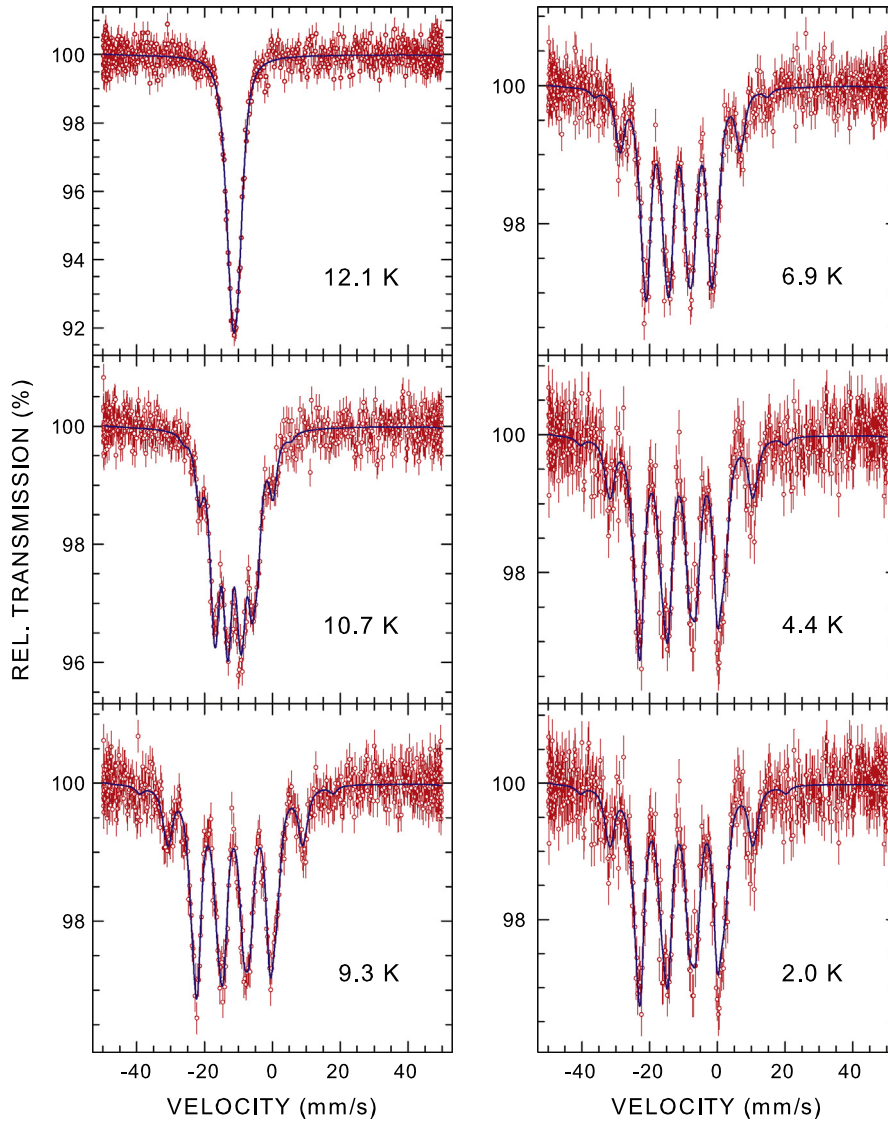


Fig. 7. Temperature dependence of (a) the principal component of the electric field gradient tensor  $V_{zz}$  and (b) the absorption spectral area  $A$  derived from the fits of the spectra in Fig. 6. The solid lines are the fits to Eq. (3) in (a) and to Eq. (4) in (b), as explained in the text.





**Fig. 8.**  $^{151}\text{Eu}$  Mössbauer spectra of  $\text{EuPdGe}_3$  obtained at the indicated temperatures, fitted (solid lines) with combined magnetic dipole and electric quadrupole hyperfine interactions, as described in the text. The zero-velocity origin is relative to the source.

its mechanism is not well understood, it is surprisingly well described by the empirical relation [103]

$$V_{zz}(T) = V_{zz}(0) \left(1 - BT^{3/2}\right), \quad (3)$$

where  $V_{zz}(0)$  is the value of  $V_{zz}$  at 0 K and  $B$  is a constant. The fit of the  $V_{zz}(T)$  data [Fig. 7(a)] to Eq. (3) yields  $V_{zz}(0) = 0.398(6) \times 10^{22} \text{ V/m}^2$  and  $B = 4.97(70) \times 10^{-5} \text{ K}^{-3/2}$ . We note that our value of  $V_{zz}(0) = 0.398(6) \times 10^{22} \text{ V/m}^2$  is almost identical to the value of  $V_{zz}(4.2 \text{ K}) = 0.39 \times 10^{22} \text{ V/m}^2$  at the Gd site in the isostructural  $\text{GdCoSi}_3$  as determined from  $^{155}\text{Gd}$  Mössbauer spectroscopy [83]. The value of  $B$  found here is similar to that found for other systems [103,107].

Fig. 7(b) displays the temperature dependence of the absorption spectral area  $A$  derived from the fits of the Mössbauer spectra in Fig. 6. This area is proportional to the absorber Debye–Waller factor  $f_a$  given [93] by

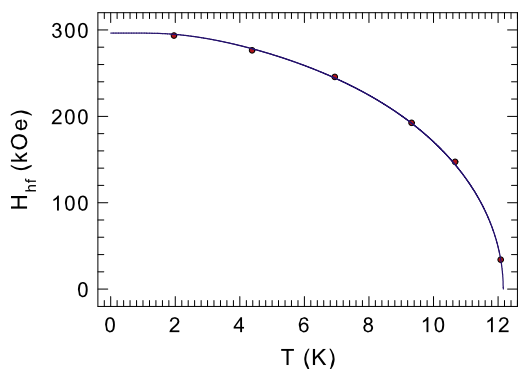
$$f_a(T) = \exp \left\{ -\frac{3}{4} \frac{E_\gamma^2}{Mc^2 k_B \Theta_D} \left[ 1 + 4 \left( \frac{T}{\Theta_D} \right)^2 \int_0^{\Theta_D/T} \frac{xdx}{e^x - 1} \right] \right\}, \quad (4)$$

where  $M$  is the mass of the Mössbauer nucleus,  $c$  is the speed of light,  $E_\gamma$  is the energy of the Mössbauer transition, and  $\Theta_D$  is the

Debye temperature. The fit of the  $A(T)$  data [Fig. 7(b)] to Eq. (4) gives  $\Theta_D = 199(2) \text{ K}$ . The value of  $\Theta_D$  found here should be compared with the value of  $268(2) \text{ K}$  derived from the specific heat data for the isostructural  $\text{EuNiGe}_3$  [90].

The  $^{151}\text{Eu}$  Mössbauer spectra of  $\text{EuPdGe}_3$  measured at temperatures at which both magnetic dipole and electric quadrupole hyperfine interactions are present are shown in (Fig. 8). The fit of the 2.0 K Mössbauer spectrum yields the following values of the hyperfine parameters:  $\delta = -11.15(5) \text{ mm/s}$ , the hyperfine magnetic field  $H_{\text{hf}} = 293.4(1.3) \text{ kOe}$ ,  $eQ_{\text{g}}V_{zz} = 4.98(87) \text{ mm/s}$ , and the angle between the direction of  $H_{\text{hf}}$  and the  $V_{zz}$ -axis  $\theta = 92(5)^\circ$ . As the principal axis of the EFG tensor ( $V_{zz}$ -axis) is along the tetragonal  $c$ -axis, the value  $\theta = 92(5)^\circ$  implies that the Eu magnetic moments in  $\text{EuPdGe}_3$  must lie in the  $ab$  plane. We note here that it was suggested [90] that the Eu magnetic moments are also aligned in the  $ab$  plane in the isostructural  $\text{EuNiGe}_3$ . Similarly, in the isostructural  $\text{GdCoSi}_3$  the Gd magnetic moments were shown with  $^{155}\text{Gd}$  Mössbauer spectroscopy to be perpendicular to the crystallographic  $c$  axis [83].

The temperature dependence of  $H_{\text{hf}}$  determined from the fits to the Mössbauer spectra in Fig. 8 is shown in Fig. 9. It is usually assumed that the temperature variation of  $H_{\text{hf}}$  in an



**Fig. 9.** Temperature dependence of the hyperfine magnetic field  $H_{\text{hf}}$  determined from the fits of the spectra in Fig. 8. The solid line is the fit to Eq. (5), as explained in the text.

antiferromagnet can be reasonably explained in term of the molecular field model, assuming that  $H_{\text{hf}}$  is proportional to the sublattice magnetization. In terms of this model,  $H_{\text{hf}}(T)$  can be expressed as

$$H_{\text{hf}}(T) = H_{\text{hf}}(0)B_J(x), \quad (5)$$

where  $H_{\text{hf}}(0)$  is the saturation hyperfine magnetic field,  $B_J(x)$  is the Brillouin function defined as

$$B_J(x) = \frac{2J+1}{2J} \coth\left(\frac{2J+1}{2J}x\right) - \frac{1}{2J} \coth\left(\frac{x}{2J}\right) \quad (6)$$

and

$$x = \frac{3J}{J+1} \frac{H_{\text{hf}}(T) T_N}{H_{\text{hf}}(0) T}. \quad (7)$$

The fit of the  $H_{\text{hf}}(T)$  data (Fig. 9) to Eq. (5) with  $J = S = 7/2$  yields  $H_{\text{hf}}(0) = 296.4(1.1)$  kOe and  $T_N = 12.16(1)$  K. We believe that the value of  $T_N$  determined here is more precise than that determined from the position of the peak in the  $\chi(T)$  data (Fig. 3).

In principle, one could attempt to estimate the saturation magnetic moment of Eu in the studied compound from the value of  $H_{\text{hf}}(0)$  found here, based on the expected proportionality between the latter and the former. The hyperfine magnetic field at the  $^{151}\text{Eu}$  nucleus in a metallic system can be written as the sum of three contributions [110]

$$H_{\text{hf}} = H_{\text{core}} + H_{\text{cep}} + H_n, \quad (8)$$

where  $H_{\text{core}}$  is the core-polarization field,  $H_{\text{cep}}$  is the contribution of the valence and conduction band electrons, and  $H_n$  includes all contributions from neighboring magnetic moments. It is only the  $H_{\text{core}}$  contribution that is truly proportional to the Eu magnetic moment. However, since all these three contributions are approximately of a similar magnitude [102], one is unable to determine the magnitude of the Eu magnetic moment from the measured value of  $H_{\text{hf}}$ .

#### 4. Conclusions

We have reported the results of X-ray diffraction, magnetic susceptibility and magnetization, and  $^{151}\text{Eu}$  Mössbauer spectroscopy measurements of the  $\text{EuPdGe}_3$  compound. The studied compound crystallizes in the  $\text{BaNiSn}_3$ -type crystal structure with the lattice constants  $a = 4.4457(1)$  Å and  $c = 10.1703(2)$  Å. The high-temperature  $\chi(T)$  data follow the modified Curie–Weiss law with a Curie constant consistent with  $\text{Eu}^{2+}$  spins  $S = 7/2$  and Weiss temperature  $\theta_p = -5.3(1)$  K indicative of dominant antiferromagnetic interactions. We find that  $\text{EuPdGe}_3$  is an antiferromagnet with the Néel temperature  $T_N = 12.16(1)$  K and the Eu ordered magnetic moments in the  $ab$  plane. The temperature dependence of

the hyperfine magnetic field is well described by a  $S = 7/2$  Brillouin function. Evidence of dynamical short-range antiferromagnetic ordering in the sample is observed in the  $M(H)$  curves on approaching  $T_N$  from above. The shape of the  $M(H)$  isotherms at temperatures below  $T_N$  is indicative of a series of field-induced first-order spin-flop transitions where the ordered magnetic moments flop to a perpendicular orientation with respect to the applied field. The principal component of the electric field gradient tensor increases with decreasing temperature and is well described by a  $T^{3/2}$  power-law relation. The Debye temperature of  $\text{EuPdGe}_3$  is found to be 199(2) K.

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