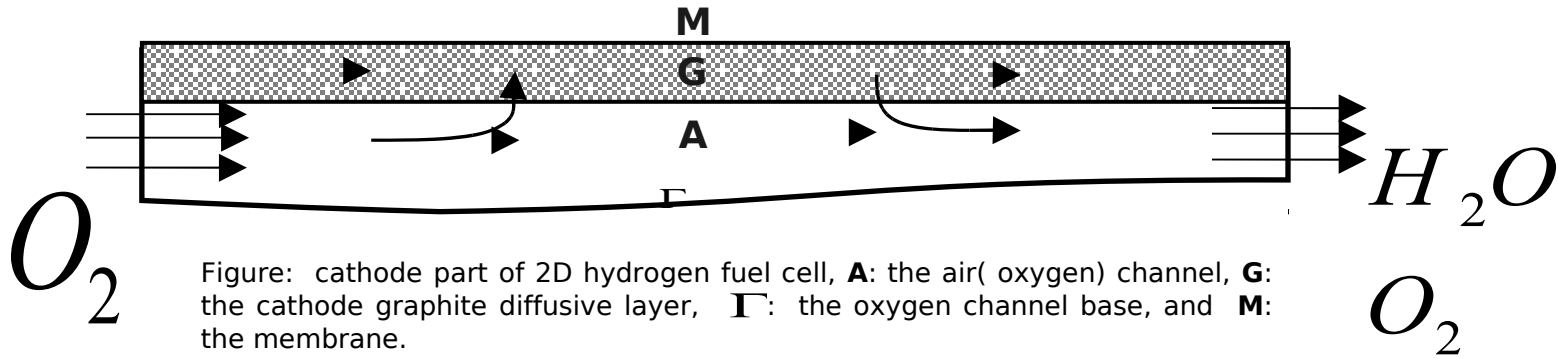


# 2D Hydrogen Fuel Cell Dry Model

## Channel Optimal Shape Design



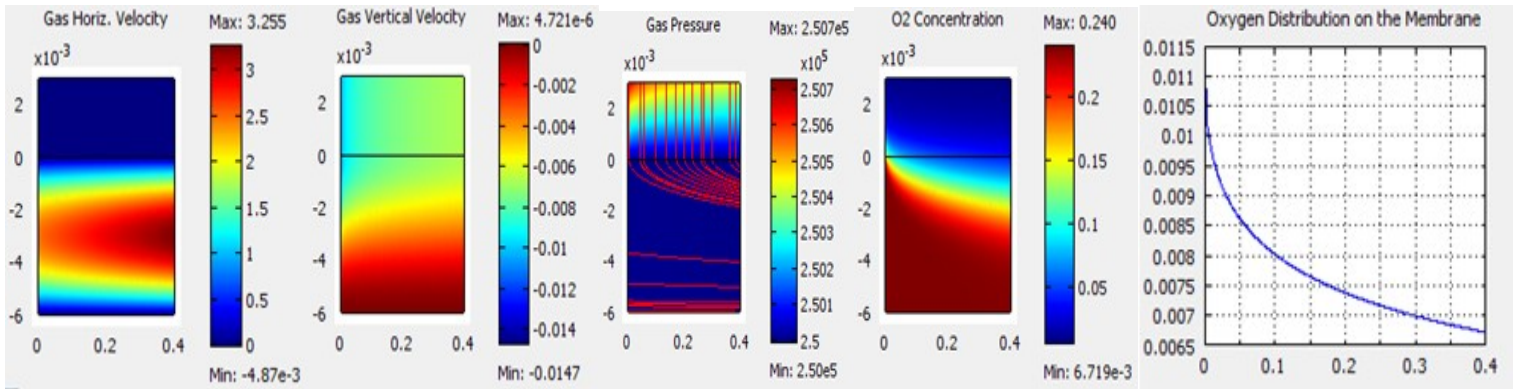
**Objective:** To design  $\Gamma$  such that the energy function,  $E$ , is minimized

$$E(\Gamma) = a \int_M (\hat{c} - \int_M \hat{c})^2 - b \int_M \hat{c}$$

Total oxygen variation on M
The

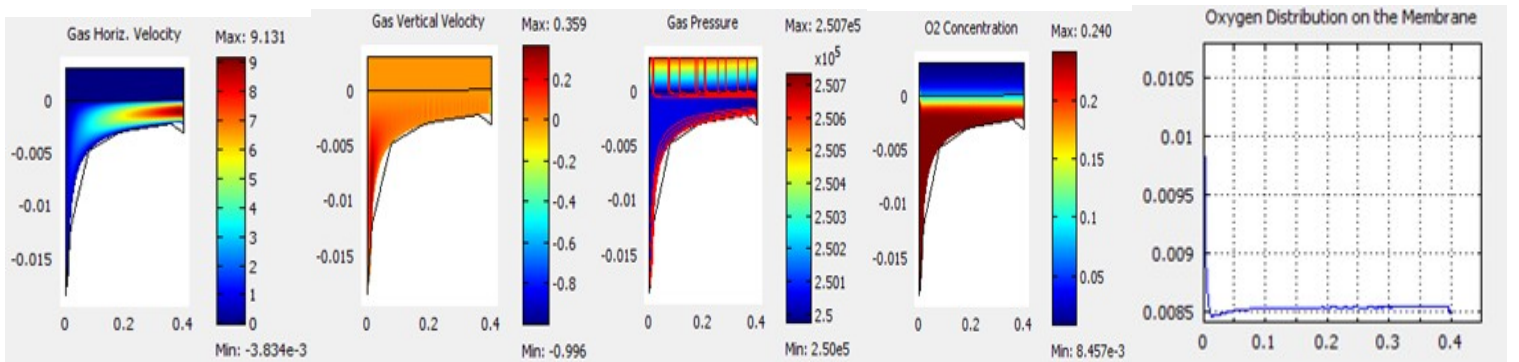
Here,  $\hat{c}$  denotes the oxygen concentration, and **a**, **b** are some nonnegative parameters.

**Initial Solution**, where  $\Gamma$  is flat:



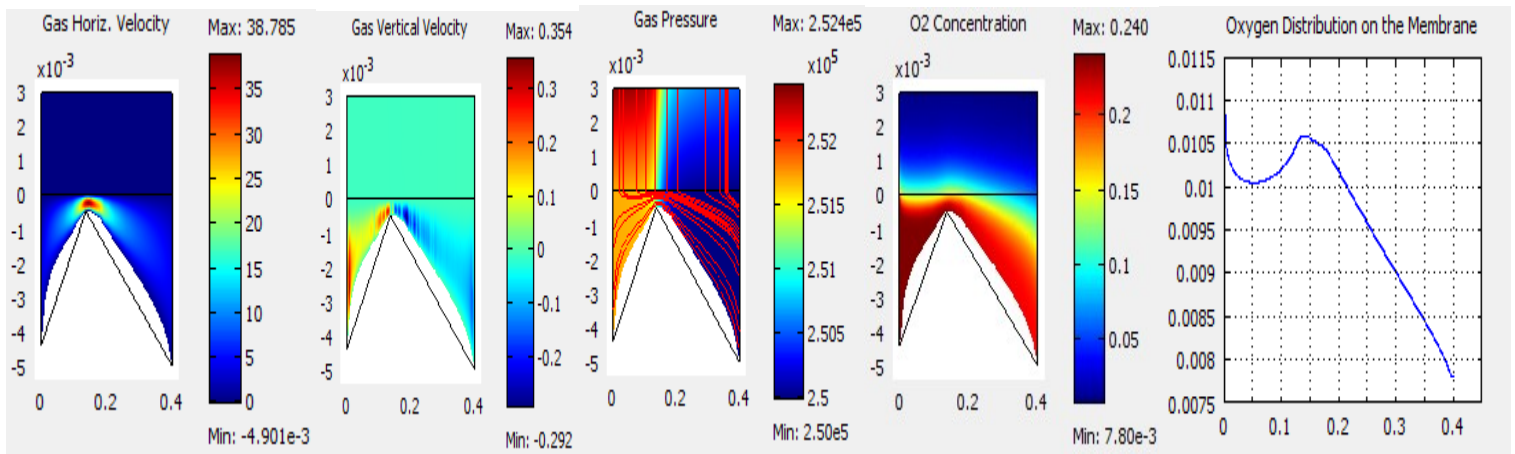
**Objective I:** How to design  $\Gamma$  such that only the total oxygen variation is minimized on the membrane, M.? That is **a=1**, **b=0**.

**Solution:**



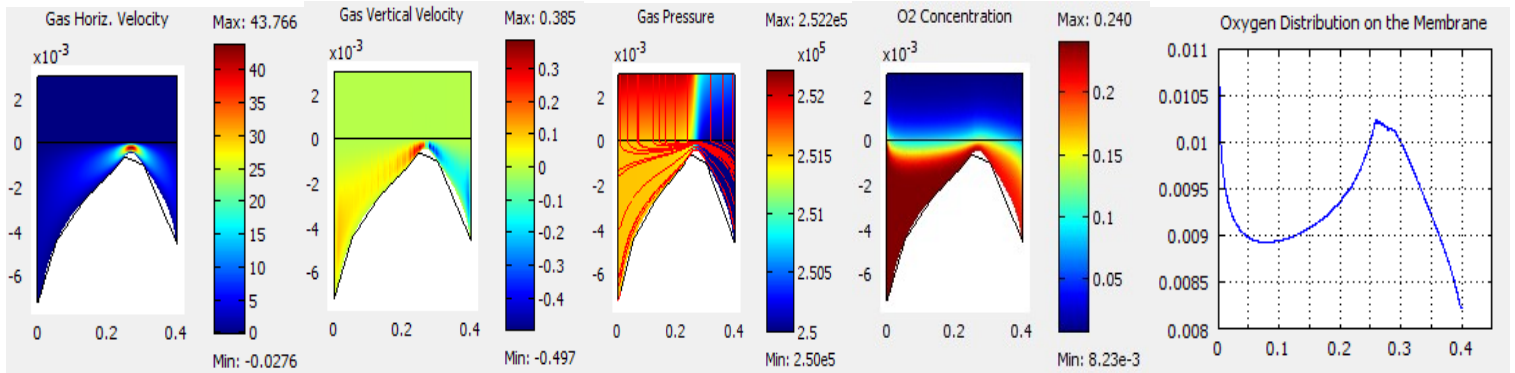
**Objective II:** How to design  $\Gamma$  such that only the total oxygen is maximized on the membrane,  $M$ ? That is  $\mathbf{b}=\mathbf{1}$ ,  $\mathbf{a}=\mathbf{0}$ .

**Solution:**

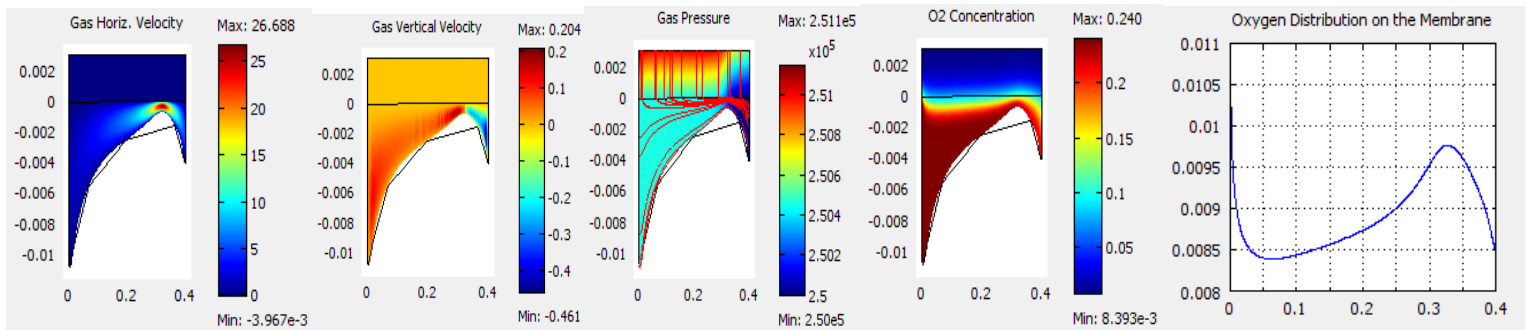


**Objective III:** To consider both **objective I** and **objective II**, with different values of the parameters  $\mathbf{a}$ ,  $\mathbf{b}$  to note the competition between the two objectives.

**Case I:  $\mathbf{a}=\mathbf{1e3}$ ,  $\mathbf{b}=\mathbf{1}$ .** In this case, **objective II** is more important than objective I.



**Case II:  $\mathbf{a}=\mathbf{5e3}$ ,  $\mathbf{b}=\mathbf{1}$ .** Here, both **objective I** and **objective II** have same importance.



**Case III:  $\mathbf{a}=\mathbf{5e4}$ ,  $\mathbf{b}=\mathbf{1}$ .** Here, **objective I** is more important than the second.

