

# Page 1

University of Ottawa

Department of Mathematics and Statistics

MAT 1341: Introduction to Linear Algebra

Instructor: Erhard Neher

Assignment 2; due June 18, 2008, 18:00 in the class room

Family Name: \_\_\_\_\_

First Name: \_\_\_\_\_

Student number: \_\_\_\_\_

Please read these instructions carefully:

- The table below is for the TA. Do not write in the table.
- The assignment has to be submitted with the two cover pages. You may or may not use the pages 3-7 of this copy.
- For privacy reasons, this page of the assignment will be detached, and you will only get back the remaining pages of the assignment. Therefore, **fill in your name on both pages and your student number on this page only.**

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Quest.	1.	2.	3.	4.	5.	Total
maximal	6	4	6	6	3 + 3 extra	25
score						

## Page 2

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Family Name: \_\_\_\_\_

First Name: \_\_\_\_\_

**Please read these instructions carefully:**

- All questions require justification, written legibly and logically: You must convince the TA and me that you know why your solution is correct. Correct answers without justification will get 0 marks.
- You have to submit this assignment at the beginning of the class on Wednesday, June 18, 2008, at 18:00 in the classroom at the latest. If you wish to submit it earlier, please do so at the secretariat of the Department of Mathematics, room 103A, 8:45–12:00 and 13:00–16:00.

**Good luck! Bonne Chance!**

1. Which of the following sets is linearly independent? If the set is dependent, give an example of a nontrivial linear combination that equals zero. You must justify your answer.

(a) (3 points)  $\{[1 \ 6]^T, [-3 \ 5]^T\}$

(b) (3 points)  $\{[1 \ -1 \ 0]^T, [3 \ 2 \ -1]^T, [5 \ 0 \ -1]^T\}$ .

2. (a) (3 points) Verify that the given vectors span  $\mathbb{R}^3$ :

$$[-5 \ -2 \ -2]^T, [7 \ -9 \ 3]^T, [4 \ -8 \ 9]^T, [8 \ 4 \ 7]^T.$$

(b) (1 point) Do the vectors form a basis of  $\mathbb{R}^3$ ?

**3. (6 points)** Show that  $U = \{[3a + 4b \quad 7a - b \quad a + b \quad -3b]^T \in \mathbb{R}^4 : a, b \in \mathbb{R}\}$  is a subspace of  $\mathbb{R}^4$ . Find a basis and  $\dim U$ .

4. (6 points) Find a basis and the dimension of  $\text{null}A$  where

$$A = \begin{bmatrix} 2 & 3 & -3 & 7 & -1 \\ 2 & 0 & 2 & 4 & -5 \end{bmatrix}.$$

5. Let  $U$  and  $V$  be any subspaces of  $\mathbb{R}^n$ .

(a) (**3 points**) Show that  $U \cap V = \{x \in \mathbb{R}^n : x \in U \text{ and } x \in V\}$  is a subspace of  $\mathbb{R}^n$ .

(b) (**3 extra points**) Show that  $U + V = \{X \in \mathbb{R}^n : X = X_U + X_V \text{ for some } X_U \in U \text{ and some } X_V \in V\}$  is also a subspace of  $\mathbb{R}^n$ .