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Enzyme Kinetics

Enzyme Catalysis

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Outline: Enzyme catalysis

- enzymes and non-bonding interactions (review)
- catalysis (review - see section 9.2 of A&D)
 - general principles of catalysis
 - differential binding
 - types of catalysis
 - approximation
 - electrostatic
 - covalent
 - acid-base catalysis
 - strain and distortion
- enzyme catalysis and energy diagrams

Enzymes

- proteins that play functional biological roles
- responsible for the catalysis of nearly all chemical reactions that take place in living organisms
 - acceleration of reactions by factors of 10^6 to 10^{17}
- biological catalysts that bind and catalyse the transformation of substrates
- the three-dimensional structures of many enzymes have been solved (through X-ray crystallography)

Reminder: Amino acid structures

- as proteins, enzymes are polymers of amino acids whose side chains interact with bound ligands (substrates)

$\begin{array}{c} \text{CO}_2\text{H} \\ \\ \text{H}_2\text{N}-\text{C}-\text{H} \\ \\ \text{R} \end{array}$		R	Name	3 Letter Code	1 Letter Code	R	Name	3 Letter Code	1 Letter Code
	H	Glycine	Gly	G	CH_2SH	Cysteine	Cys	C	
	CH_3	Alanine	Ala	A	$\text{CH}_2\text{CH}_2\text{SCH}_3$	Methionine	Met	M	
	$\text{CH}(\text{CH}_3)_2$	Valine	Val	V	$(\text{CH}_2)_4\text{NH}_2$	Lysine	Lys	K	
	$\text{CH}_2\text{CH}(\text{CH}_3)_2$	Leucine	Leu	L	$(\text{CH}_2)_3\text{NHCNH}_2$	Arginine	Arg	R	
	$\begin{array}{c} \text{CHCH}_2\text{CH}_3 \\ \\ \text{CH}_3 \end{array}$	Isoleucine	Ile	I	$\begin{array}{c} \text{H}_3\text{C} \\ \\ \text{N} \\ \\ \text{H} \end{array}$	Histidine	His	H	
	$\text{CH}_2-\text{C}_6\text{H}_5$	Phenylalanine	Phe	F	$\begin{array}{c} \text{H}_3\text{C} \\ \\ \text{N} \\ \\ \text{H} \end{array}$	Tryptophan	Trp	W	
	$\begin{array}{c} \text{CO}_2\text{H} \\ \\ \text{HN} \\ \\ \text{CH}_2 \end{array}$	Proline	Pro	P	$\begin{array}{c} \text{O} \\ \\ \text{CH}_2\text{COOH} \end{array}$	Aspartic acid	Asp	D	
	CH_2OH	Serine	Ser	S	$\begin{array}{c} \text{O} \\ \\ \text{CH}_2\text{CNH}_2 \end{array}$	Asparagine	Asn	N	
	$\begin{array}{c} \text{CHOH} \\ \\ \text{CH}_3 \end{array}$	Threonine	Thr	T	$\begin{array}{c} \text{O} \\ \\ \text{CH}_2\text{CH}_2\text{COOH} \end{array}$	Glutamic acid	Glu	E	
	$\text{CH}_2-\text{C}_6\text{H}_4-\text{OH}$	Tyrosine	Tyr	Y	$\begin{array}{c} \text{O} \\ \\ \text{CH}_2\text{CH}_2\text{CNH}_2 \end{array}$	Glutamine	Gln	Q	

Coenzymes and cofactors

- indispensable for the activity of some enzymes
- can regulate enzymatic activity
- the active enzyme-cofactor complex is called a *holoenzyme*
- an enzyme without its cofactor is called an *apoenzyme*

Cofactors

- metal ions (Mg^{2+} , Mn^{2+} , Fe^{3+} , Cu^{2+} , Zn^{2+} , etc.)
- three possible modes of action:
 1. primary catalytic centre
 2. facilitate substrate binding (through coordination bonding)
 3. stabilise the three-dimensional conformation of an enzyme

Coenzymes

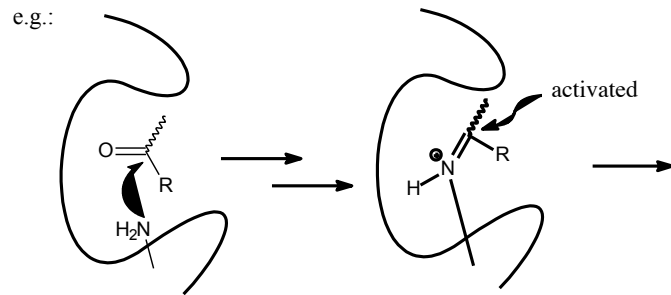
- organic molecules, very often vitamins
 - e.g.: nicotinic acid gives NAD; pantothenic acid gives CoA
- intermediates in the transport of functional groups
 - e.g. H (NAD), acyl (CoA), CO₂ (biotin), etc
- also known as *prosthetic groups*

Protein-ligand interactions

- covalent bonds
- ionic bonds
- ion-dipole and dipole-dipole interactions
- hydrogen bonds
- charge transfer complexes
- hydrophobic interactions
- van der Waals interactions

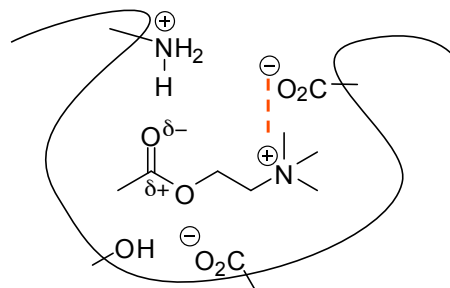
Covalent bond

- the formation of a covalent bond can represent a stabilisation of 40 to 110 kcal/mol



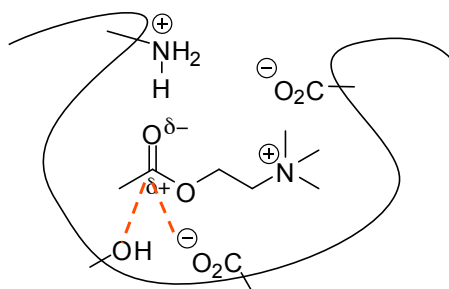
Ionic bonds

- Coulombic attraction between full positive and negative charges
 - ~5 kcal/mol of stabilisation



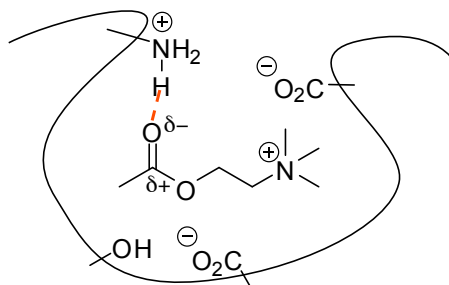
Ion-dipole and dipole-dipole interactions

- electrostatic interactions that involve partial charges
 - ~1 kcal/mol of stabilisation



Hydrogen bonds

- special type of dipole-dipole interaction
 - donors / acceptors : N, O, F
 - stabilisation of around 3-10 kcal/mol

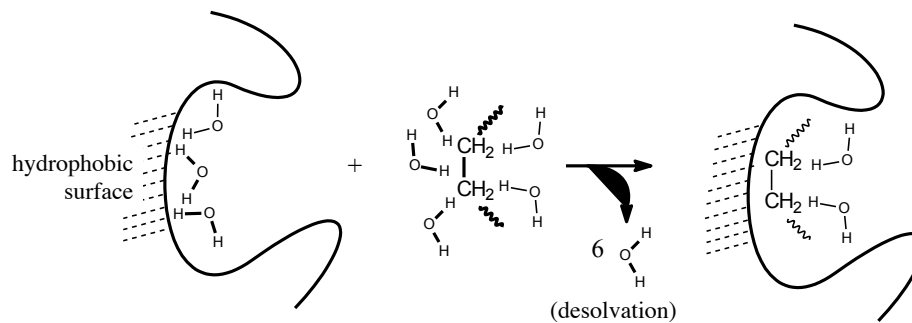


Charge transfer complex

- special type of dipole-dipole interaction
- involves π electrons, often in aromatic rings (Phe, Tyr, Trp, His)
 - stabilisation : < 3 kcal/mol

Hydrophobic interactions

- stabilisation largely due to desolvation (entropy increase)
 - stabilisation : ~ 0.5 kcal/mol



van der Waals interactions

- special type of dipole-dipole interaction
 - movement of electrons in electron cloud of alkyl chains induces the formation of temporary dipoles
 - very important over short distances
 - stabilisation : ~ 0.5 kcal/mol (per interaction)

Outline: General principles of catalysis

- see section 9.1 of A&D
 - principles of catalysis
 - differential bonding

General principles

- a **catalyst** accelerates a reaction without being consumed
- the rate of catalysis is given by the **turnover number**
- a reaction may alternatively be “**promoted**” (accelerated, rather than catalysed) by an **additive** that is consumed
- a **heterogeneous** catalyst is not dissolved in solution; catalysis typically takes place on its surface
- a **homogeneous** catalyst is dissolved in solution, where catalysis takes place
- all catalysis is due to a **decrease in the activation barrier, ΔG^\ddagger**

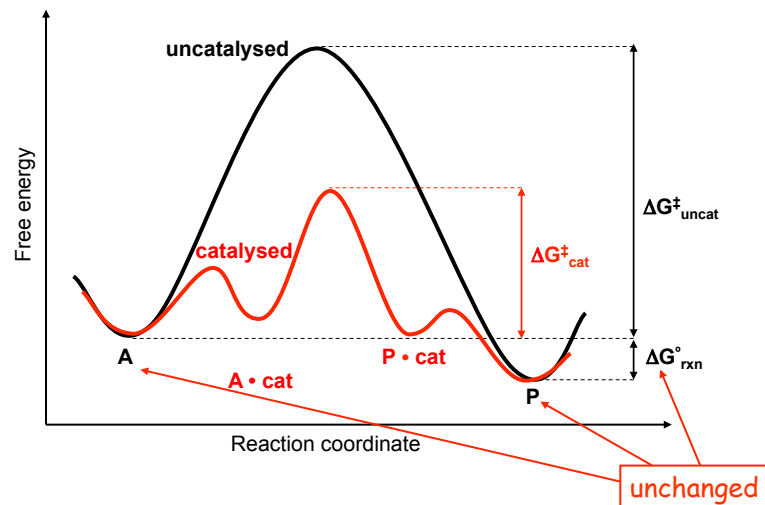
Catalysts

- efficient at low concentrations
 - e.g. $[\text{Enz}]_{\text{cell}} \ll 10^{-5} \text{ M}$; $[\text{Substrates}]_{\text{cell}} < 10^{-4} - 10^{-5} \text{ M}$
- not consumed during the reaction
 - e.g. each enzyme molecule can catalyse the transformation of $20 - 36 \times 10^6$ molecules of substrate per minute
- do not affect the equilibrium of reversible chemical reactions
 - only accelerate the rate of approach to equilibrium end point
- most chemical catalysts operate in extreme reaction conditions while enzymes generally operate under mild conditions ($10^\circ - 50^\circ \text{ C}$, neutral pH)
- enzymes are specific to a reaction and to substrates; chemical catalysts are far less selective

Catalysis and free energy

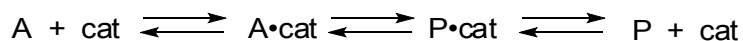
- catalysis accelerates a reaction by stabilising a TS relative to the ground state
 - free energy of activation, ΔG^\ddagger , *decreases*
 - rate constant, k , *increases*
- catalysis does not affect the end point of an equilibrium, but only accelerates how quickly equilibrium is attained
 - free energy of the reaction, ΔG° , *remains unchanged*
 - equilibrium constant, K_{eq} , *remains unchanged*

Energy profile of catalysis



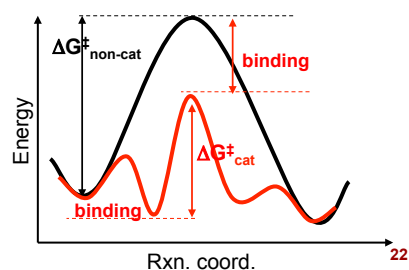
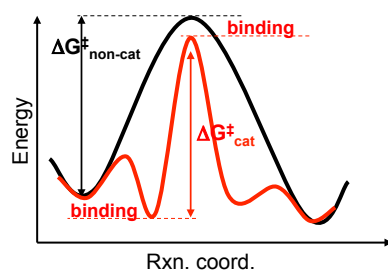
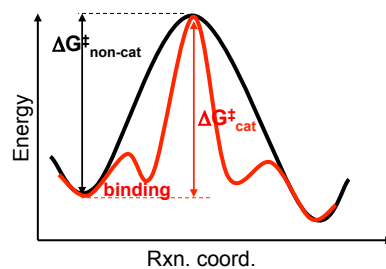
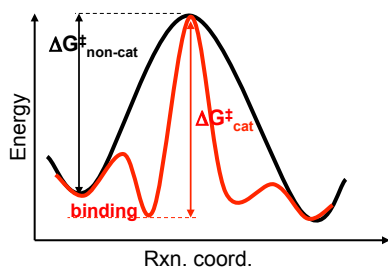
Transition state binding

- interaction between a catalyst and reactant or activated complex can stabilise one or the other
- if the activated complex is bound more strongly than the substrate, the activation barrier will be decreased
- HOWEVER, the activated complex is not a molecule – so the catalysts must first of all interact with the substrate, and then release the product at the end of the reaction :



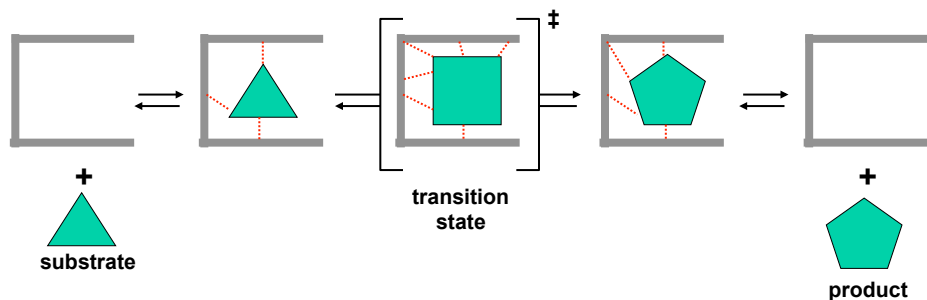
Differential binding

- consider 4 scenarios :



Differential binding

- to accelerate a reaction, a catalyst must stabilise the TS more than it stabilises the substrate
 - even if this stabilisation takes place over less time than that of a bond vibration, by definition



Outline: Types of catalysis

- see section 9.2 of A&D
 - approximation
 - electrostatic
 - covalent
 - strain and distortion

Catalysis by approximation

- the catalyst *brings together* the reactants, increasing their *effective concentrations*, and *orients* them with respect to the reactive groups

Jencks :

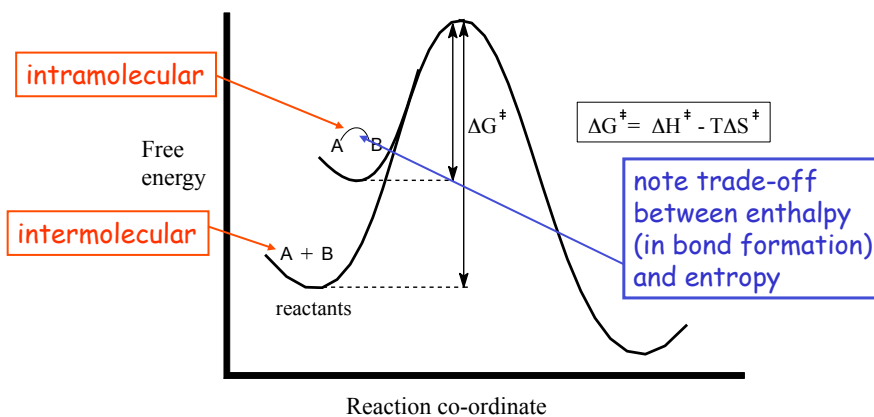
- the loss of entropy associated with the restriction of rotation and translation of substrate must be compensated by the *intrinsic energy of binding* (favourable non-bonding interactions)

Bruice / Kirby :

- the magnitude of this effect is given by the *effective concentration*, determined by comparison of the rate constants of the bimolecular and intramolecular reactions

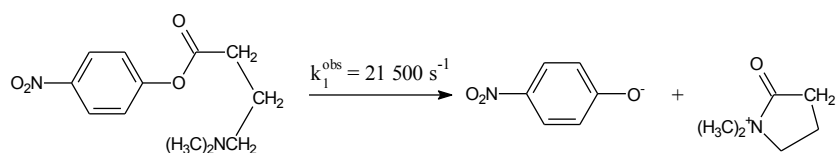
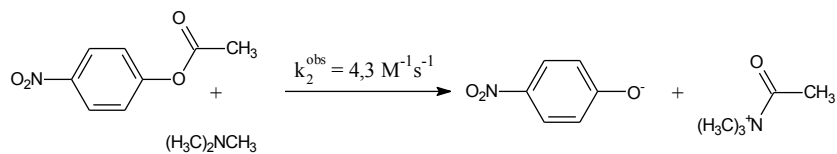
Intramolecular approximation

- an intramolecular reaction implies a smaller decrease in entropy (and therefore a decrease in the free energy of activation)



Example of catalysis by approximation

- the catalyst *brings together* the reactants, increasing their *effective concentrations*, and *orients* them with respect to the reactive groups



$$\frac{k_1^{\text{obs}}}{k_2^{\text{obs}}} = 5000 \text{ M} = \text{effective concentration, or effective molarity (EM)}$$

Example: Ester hydrolysis

parent reaction

Reaction	k_{rel}	Effective concentration (M)
<chem>CC(=O)OAr</chem> + <chem>CC(=O)O[O-]</chem>	$1 \text{ M}^{-1} \text{ s}^{-1}$	-
<chem>CC(=O)OAr</chem> + <chem>CC(=O)O[O-]</chem>	220 s^{-1}	220 M
<chem>CC(=O)OAr</chem> + <chem>CC(=O)O[O-]</chem>	$5.1 \times 10^4 \text{ s}^{-1}$	$5.1 \times 10^4 \text{ M}$
<chem>CC(=O)OAr</chem> + <chem>CC(=O)O[O-]</chem>	$2.3 \times 10^6 \text{ s}^{-1}$	$2.3 \times 10^6 \text{ M}$
<chem>CC(=O)OAr</chem> + <chem>CC(=O)O[O-]</chem>	$1.2 \times 10^7 \text{ s}^{-1}$	$1.2 \times 10^7 \text{ M}$

decreasing entropy of rotation and translation

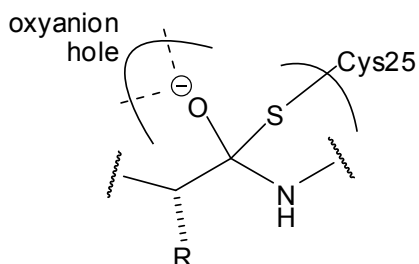
More notions of catalysis by approximation

- many notions have been advanced by many different researchers, to describe the subtleties of catalysis by approximation:
 - *orbital steering*: the alignment of orbitals is proposed to accelerate the reaction
 - *stereopopulation control*: one reactive conformer among several is favoured
 - *near attack conformations*: conformations are favoured whose spatial orientation lead to the desired reaction

CAUTION: one must not forget the Curtin-Hammett principle!!

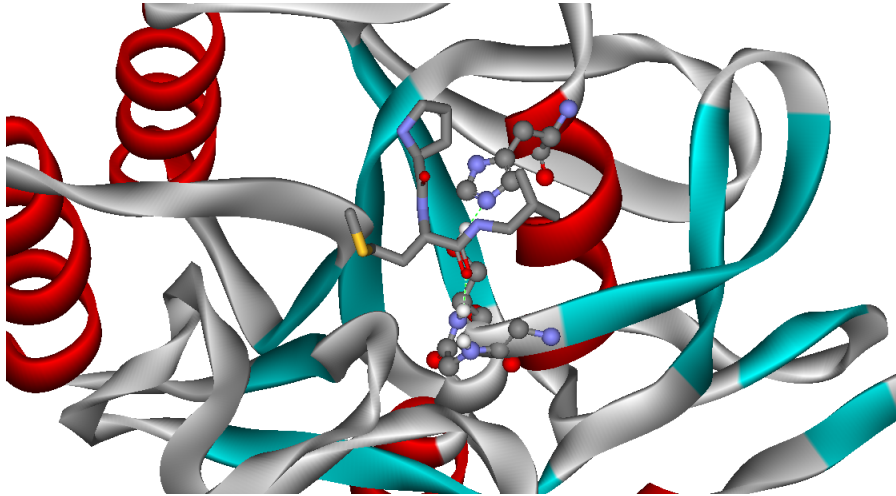
Electrostatic catalysis

- stabilisation of charge developed at TS
- for example, serine and cysteine proteases favour the formation of a tetrahedral intermediate by stabilising the negative charge developed on oxygen, in an *oxyanion hole*
 - e.g.: consider papain, a Cys protease



Electrostatic catalysis

- e.g.: oxyanion hole of subtilisin:



Electrostatic catalysis

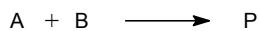
- can be very important :
 - consider the triple mutant of subtilisin where each residue of its catalytic triad is replaced (S221A-H64A-D32A)
 - catalyses proteolysis 10^6 -fold less than the native enzyme
 - BUT the reaction with the mutant is still 10^3 -fold faster than the uncatalysed reaction!!
 - an important part of catalysis is due to the electrostatic environment

Metal catalysis

- electrostatic charges developed at the TS can also be stabilised by metal ions
- coordination of a ligand by a metal (as a Lewis acid) can also lead to polarisation of a ligand
 - e.g. pK_a of metal-bound H_2O is 7.2, making it easier to deprotonate, thereby generating $-OH$ as a nucleophile
 - for example, zinc-bound water in carbonic anhydrase, a highly efficient metalloenzyme as well as certain enzyme models

Covalent catalysis

- catalyst forms a covalent intermediate that reacts faster than uncatalysed reaction :



vs

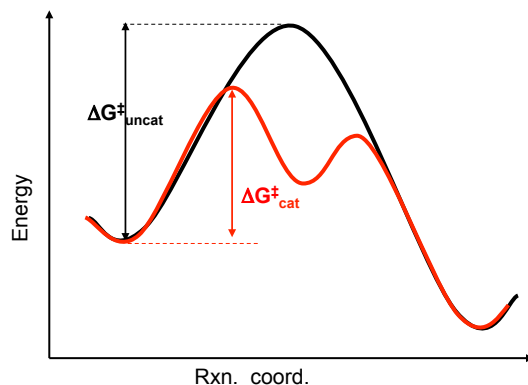


intermediate

more reactive

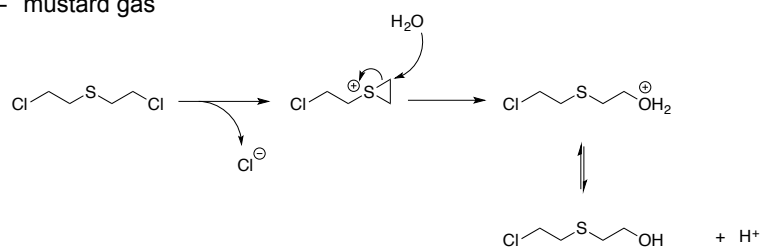
Covalent catalysis

- in order for catalysis to be efficient, the activation energy for formation of the intermediate and for its subsequent reaction must both be lower than that of the uncatalysed reaction :



Covalent catalysis

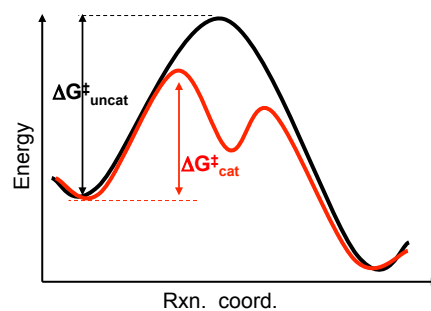
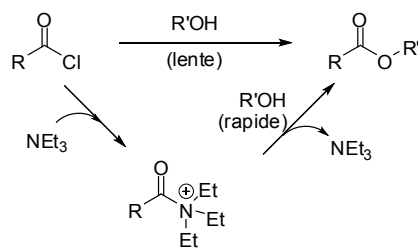
- an example of non-enzymatic covalent catalysis and *anchimeric assistance* :
 - mustard gas



- enzymes use nucleophilic groups (e.g. Asp, Glu, Ser, Cys, Lys, His, Arg) and cofactors to form covalent bonds (*nucleophilic catalysis*)

Nucleophilic catalysis

- catalyst attacks substrate to form intermediate that is even more susceptible to nucleophilic attack, by a second reactant
 - e.g. reaction of acid chlorides with alcohols, catalysed by addition of a tertiary amine:



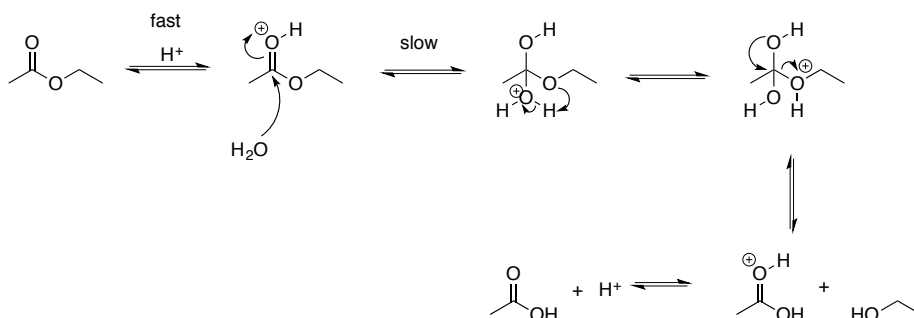
Acid-base catalysis

- the catalyst (namely an acid or a base) accelerates the reaction through *protonation* or *deprotonation*

Specific acid-base catalysis

- catalysis by H^+ or -OH , controlled only by pH, where a *fast equilibrium* precedes the rls :

- e.g.:

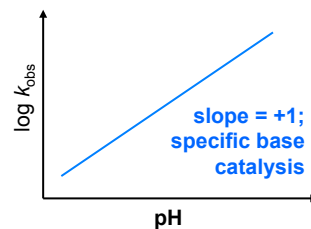
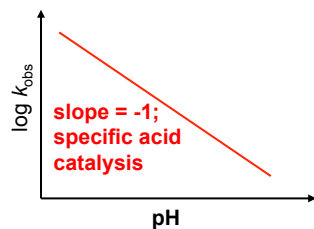


Rate laws of specific acid-base catalysis

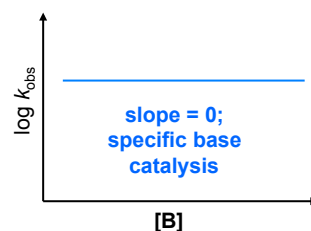
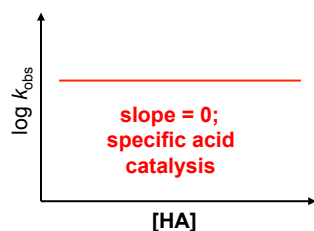
- when a substrate must be protonated *before* its reaction in the rls, this appears as a pH dependence in the rate law:
 - e.g.: $v = k[\text{R}]\times[\text{H}^+]/K_{\text{a,RH}}$
- when a substrate must be deprotonated *before* its reaction in the rls, this appears as a pH dependence in the rate law:
 - e.g.: $v = k[\text{RH}]\times K_{\text{a,RH}}/[\text{H}^+]$

Specific acid-base catalysis plots

- pH dependence :



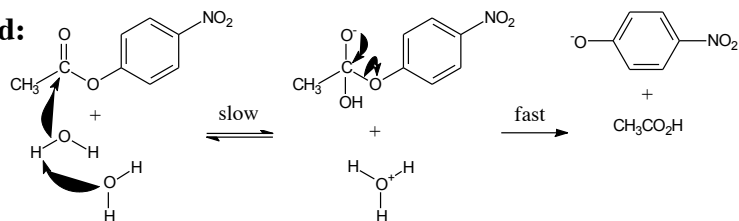
- at constant pH, independence of [HA] or [B] :



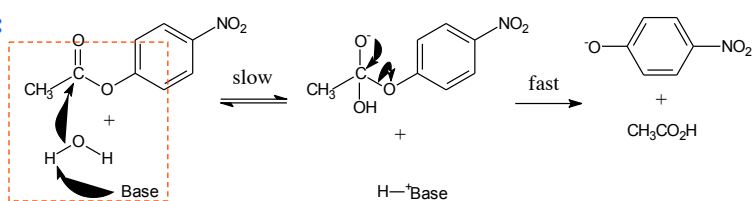
General acid catalysis

- catalysis by an acid or a base (not H^+ nor OH^-) where a proton is transferred *during the rls*
 - rate is proportional to the concentration of acid or base, at constant pH

uncatalysed:



catalysed:

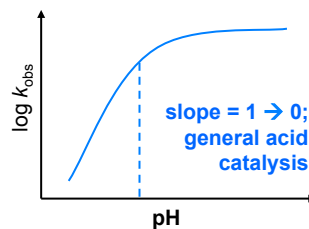
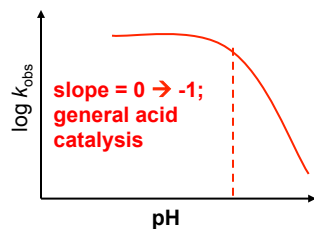


Rate laws

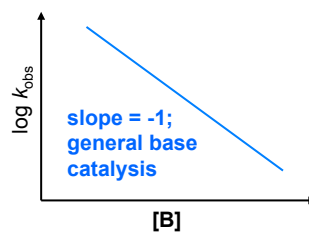
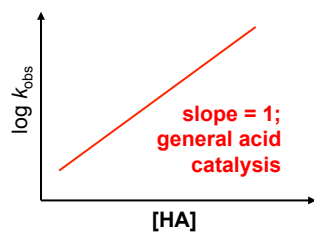
- if a substrate is protonated *during* the rls, this appears as a dependence on [HA] in the rate law :
 - e.g.: $v = k[R] \times [HA] \rightarrow = k_{\text{obs}}[R]$ where $k_{\text{obs}} = k[HA]$
- if a substrate is deprotonated *during* the rls, this appears as a dependence on [B] in the rate law:
 - e.g.: $v = k[R] \times [B] \rightarrow = k_{\text{obs}}[R]$ where $k_{\text{obs}} = k[B]$

General acid-base catalysis plots

- pH dependence :

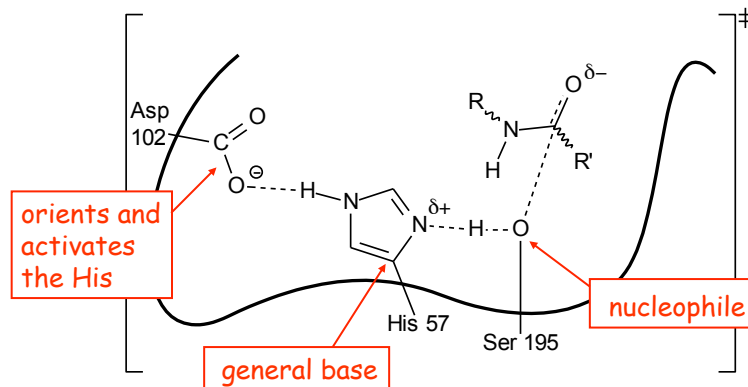


- at constant pH, dependence on [HA] or [B]:



General acid-base catalysis

- very common in enzymes
 - e.g. chymotrypsin uses a catalytic triad whose His plays the role of a general base :



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Strain and distortion

- *destabilisation of the ground state* induced in the substrate **or** in the catalyst (such as an enzyme)

Koshland :

- *induced complementarity* hypothesis: the approach of substrate serves to provoke a conformational change in the enzyme, to adopt a form that better binds the substrate, but in a higher energy (strained) form and/or to better orient reactive groups ("*orbital steering*")
- the substrate can also be deformed to adopt a strained form

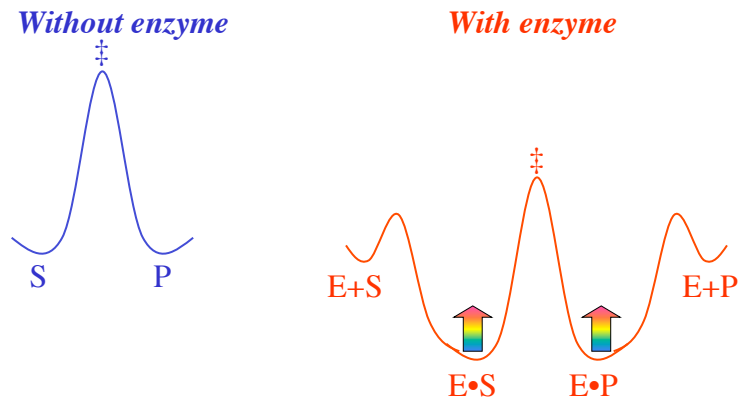
Jencks :

- strain and distortion in the substrate are *essential* for the catalysis
- TSs are stabilised, rather than E•S and E•P complexes (so as not to form overly stable intermediates)
- *binding energy must therefore be used to destabilise* the E•S and E•P complexes

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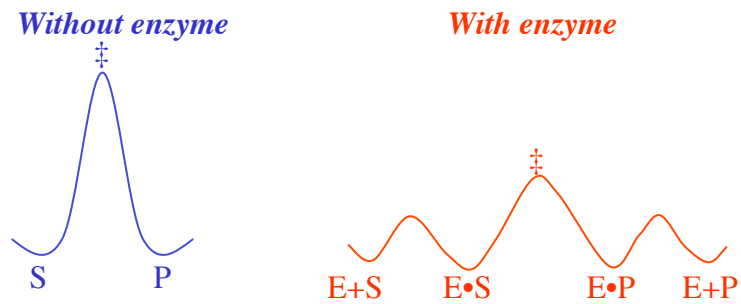
Strain and distortion

- *binding energy is used to destabilise the E•S and E•P complexes*



Strain and distortion

- *binding energy is used to destabilise the E•S and E•P complexes*



Productive strain

- in order for a reaction to be facilitated by strain, two conditions must be met:
 1. the strain must be along the reaction pathway
 - strain “pushes” the reactants towards the TS
 2. the strain must be at least partly alleviated at the TS
 - if the strain were still present at the TS, it would not contribute to catalysis

Enzymes as catalysts

Jencks :

- enzymes use *binding* energy to effect catalysis

Wolfenden :

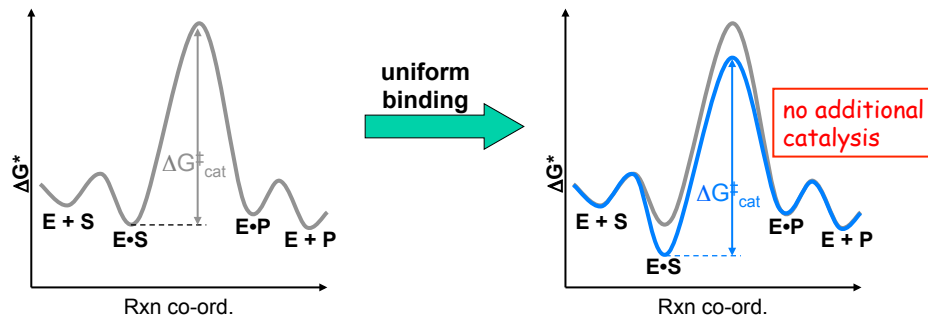
- reaction acceleration is proportional to the affinity of an enzyme for the *transition state* of the catalysed reaction
- the reaction rate is proportional to the concentration of *substrate in the activated complex* at the TS
- substrate affinity is therefore also important and enzymes use *protein conformational changes* during the reaction to better *stabilise* the TS

Knowles :

- often the various steps of an enzymatic reaction are stabilised so as to *level* the energies of the various ground states and TSs

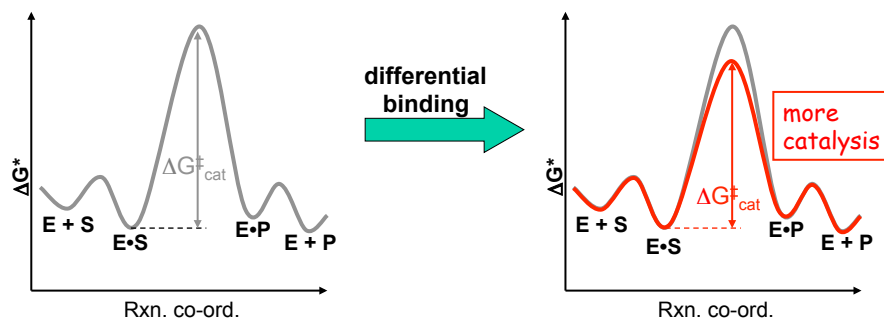
Energy diagrams

- consider energy profiles for enzymatic reactions, at the native concentration of substrates:
- for $K_M \ll [S]$ (binding of substrate heavily favoured)
 - the *uniform* binding of substrate and activated complex would not lead to catalysis :



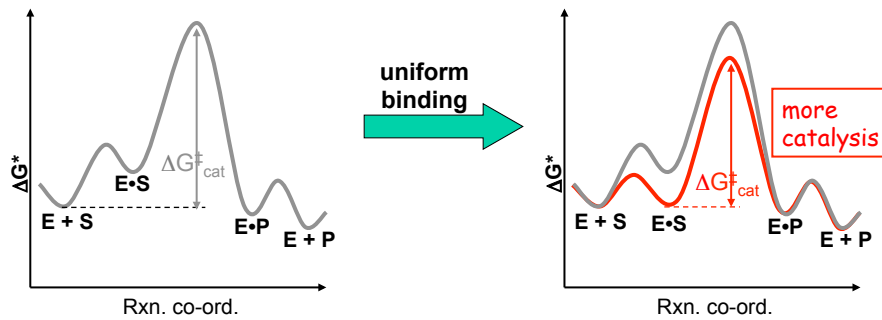
Energy diagrams

- consider energy profiles for enzymatic reactions, at the native concentration of substrates:
- for $K_M \ll [S]$ (binding of substrate heavily favoured)
 - the *differential* binding of substrate and activated complex can lead to catalysis :



Energy diagrams

- consider energy profiles for enzymatic reactions, at the native concentration of substrates:
- for $K_M > [S]$ (binding of substrate *not* favoured)
 - the *uniform* binding of substrate and activated complex can lead to catalysis :



Energy diagrams

- consider energy profiles for enzymatic reactions, at the native concentration of substrates:
- for $K_M > [S]$
 - the *differential* binding of substrate and activated complex can lead to catalysis :

