

**Calculus for the Life Science I**  
**MAT1330A , MAT1330B, MAT1330E**  
**Assignment 5**

Due date: Oct. 28

Instructor (circle one):    Jing Li    ,    Catalin Rada    ,    Frithjof Lutscher

DGD (circle one):    1    ,    2    ,    3    ,    4

Student Name (printed): \_\_\_\_\_

Student ID Number: \_\_\_\_\_

**Question 1**

Consider the function  $f(x) = x^{5/3}e^{-x}$ .

a) Find the roots of  $f$  to complete the following table.

$x$	
$f(x)$	

b) Compute the derivative of  $f$ .

$f'(x) =$

c) Find the critical points of  $f$  to complete the following table.

$x$	
$f'(x)$	
description <sup>1</sup>	

d) Compute the second derivative of  $f$ .

$f''(x) =$

e) Find the inflection points of  $f$  to complete the following table.

---

<sup>1</sup>Determine where the function is increasing or decreasing, if there are local minimums or local maximums, ...

$x$	
$f''(x)$	
description <sup>2</sup>	

f) Draw the graph of  $f$ .



### Question 2

Find the global maximum and minimum of  $f(x) = \frac{x-1}{x^2+8}$  on the interval  $[0, 6]$ .

Global maximum of  at  $x =$  .

Global minimum of  at  $x =$  .

### Question 3

The size of a population as a function of time is given by the function

$$p(t) = 5000 + \frac{200t}{10+t^3}, \quad t \geq 0.$$

Find the global minimum and maximum of this function for  $t \geq 0$ .

Global maximum of  at  $x =$  .

Global minimum of  at  $x =$  .

---

<sup>2</sup>Determine if the function is concave up or down, if there are inflection points, ...